

# PropertyDAG: Multi-Objective Bayesian Optimization for Biological Sequence Design



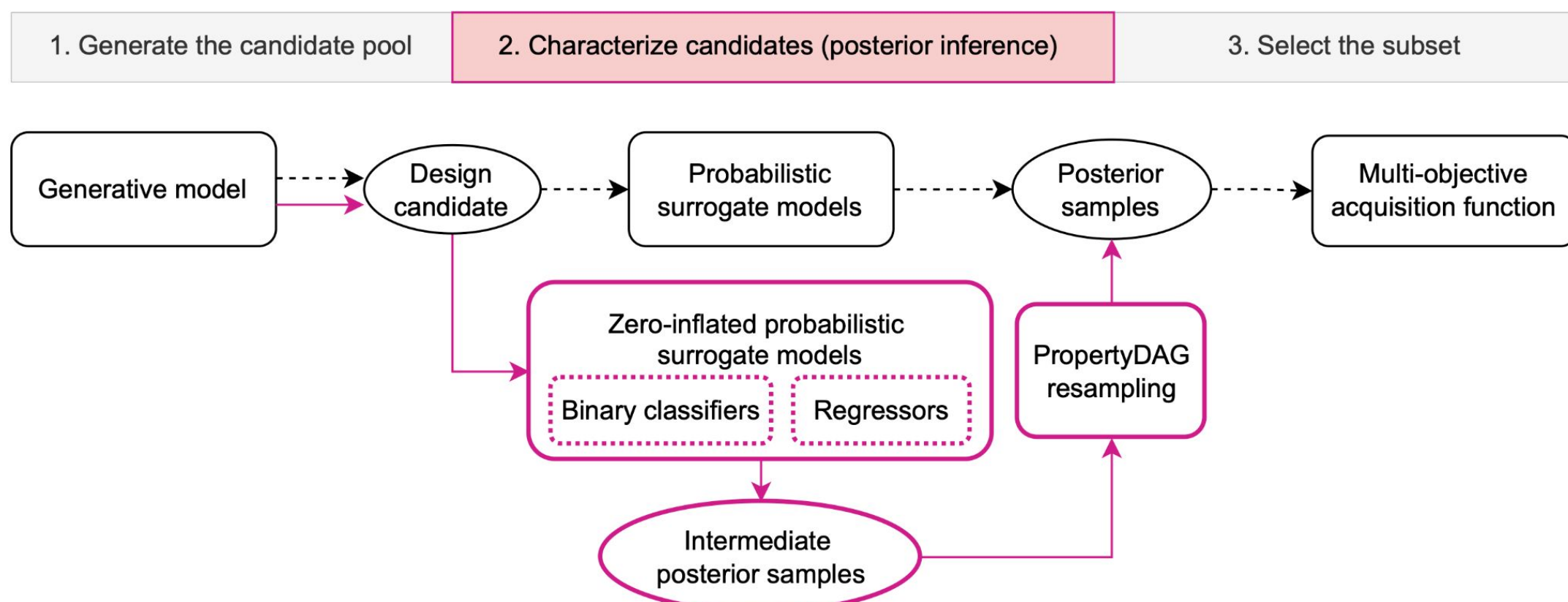
Prescient  
Design  
A Genentech Accelerator

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## Motivation

- *In silico* drug design involves fulfilling property desiderata such as expression/synthesizability, potency against a therapeutic target, and various developability properties [1, 2].
- Sequential nature of wet-lab characterization inspires optimization conditioned on preceding properties satisfying some constraints.
- Multi-objective Bayesian optimization (BO) offers a principled framework for navigating the exploration-exploitation trade-off in design space across multiple properties.
- Acquisition functions like expected hypervolume improvement (EHVI) [3] provide Pareto fronts with excellent coverage [4] but do not allow discrimination between different regions on the Pareto frontier.

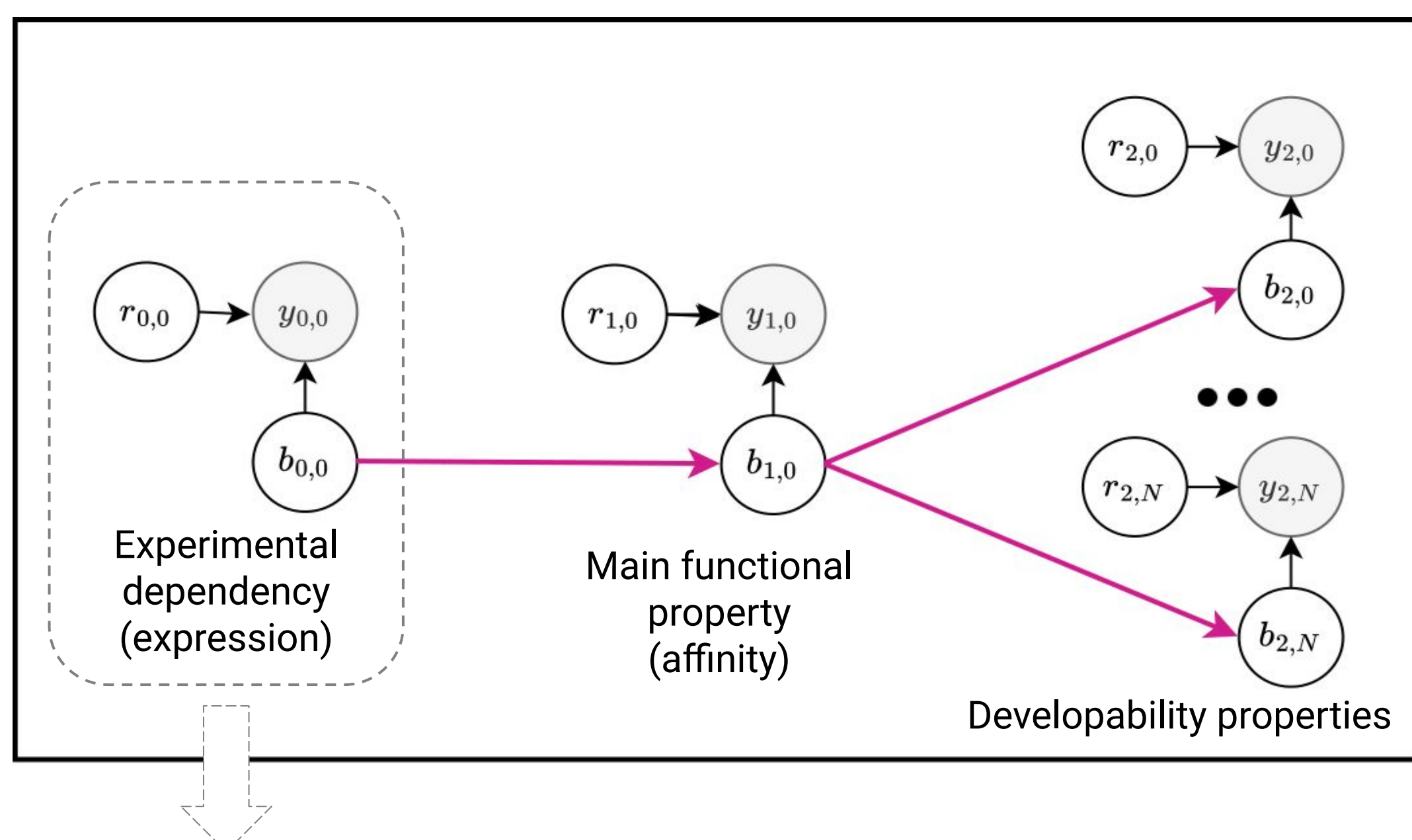
## Method



**PropertyDAG-BO pipeline.** Traditional multi-objective BO pipeline (dashed black) compared to PropertyDAG-BO (magenta) modifying the posterior inference step.

### 1. Choosing a PropertyDAG

Assign experimental dependencies (e.g., expression → affinity) or prioritized properties (e.g., affinity → specificity, stability) as parents.



### 2. Zero-inflated modeling with PropertyDAG

Characterize each property with a probabilistic classifier (e.g., does the antibody bind to the antigen?) and a probabilistic regressor for the positives only (e.g., what is the affinity, if it does bind?).

Modify their posterior distributions so that a given property is zero if any of its predecessor properties is zero:

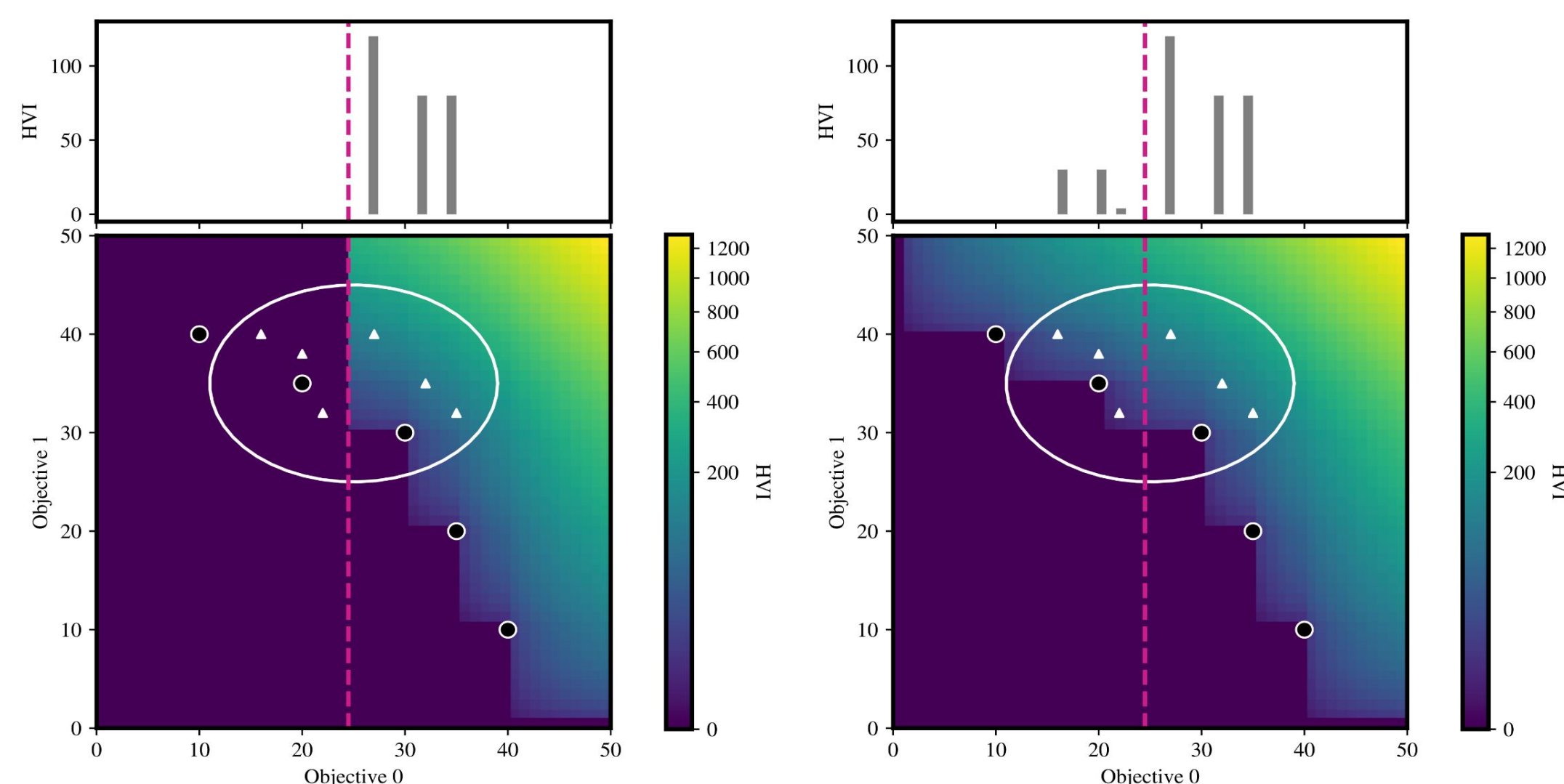
$$p(b_k | \mathbf{x}, \mathcal{D}_t) = \begin{cases} 0 & \text{if } \exists j \in \text{pred}(k) \text{ s.t. } b_j = 0, \\ p(b_k | \mathbf{x}, \mathcal{D}_t, \theta_b) & \text{else,} \end{cases}$$

Classifier

$$p(\hat{f}_k(\mathbf{x}) = c | \mathcal{D}_t) = \begin{cases} p(b_k = 0 | \mathbf{x}, \mathcal{D}_t) & \text{if } c = 0, \\ p(b_k = 1 | \mathbf{x}, \mathcal{D}_t) p(r_k = c | \mathbf{x}, \mathcal{D}_t, \theta_r) & \text{else,} \end{cases}$$

Regressor

## PropertyDAG-EHVI



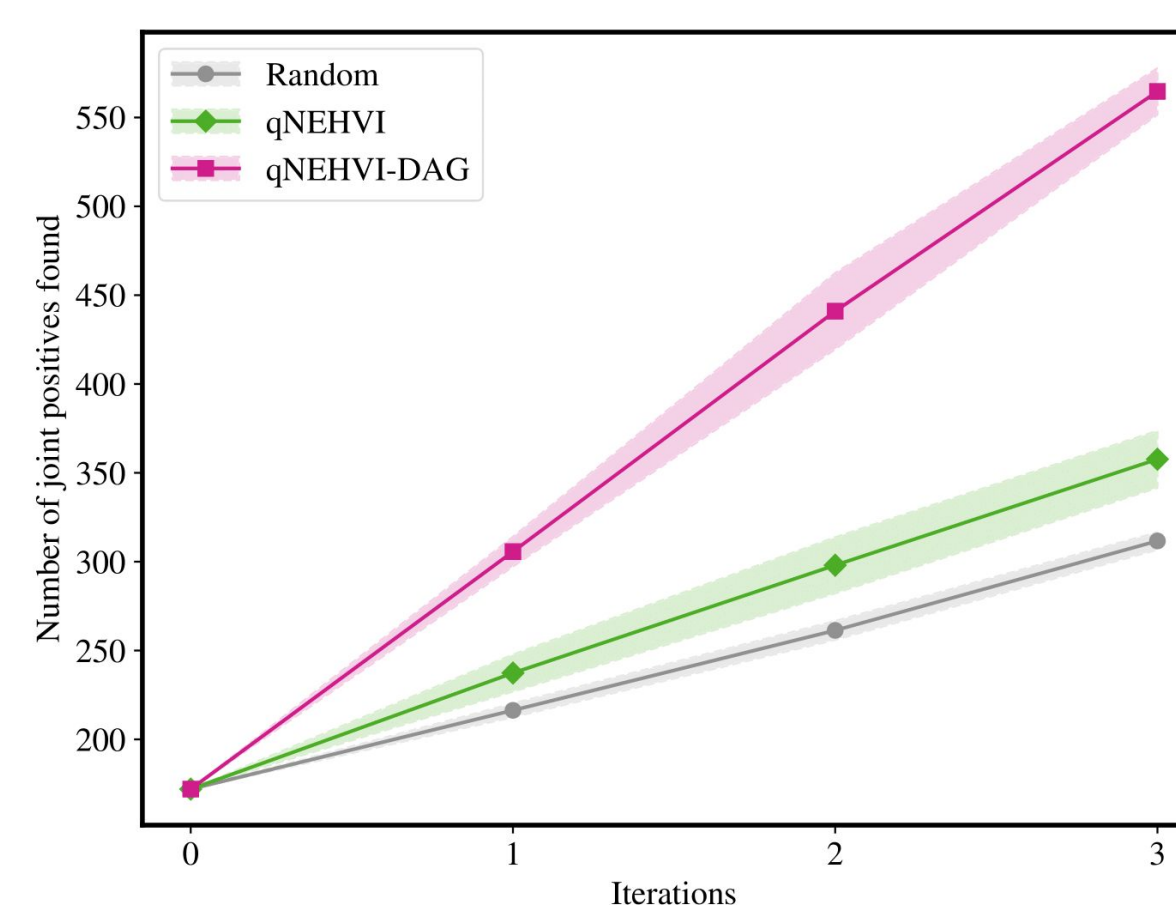
Say we want designs that maximize Objective 1 and exceed a threshold (dashed magenta) in Objective 0, given some baseline (black dots). Consider six samples (white triangles) from the posterior (white contour). PropertyDAG transforms the posterior samples below the threshold so that their HVI contribution is zero.

## Experiments

PropertyDAG for antibody design: expression (Obj 0, binary) → affinity (Obj 1, zero-inflated, continuous).

We simulate 3 iterations of active learning by splitting a dataset of antibody scFv sequences and associated expression and affinity labels into 5 groups.

Initial training set (N = 1,230)	Pool 1 (N = 736)	Pool 2 (N = 746)	Pool 3 (N = 711)	Test set (N = 600)
Initializes surrogates	Select 200 in iteration 1 from this pool	Select 200 in iteration 2 from this pool	Select 200 in iteration 3 from this pool	Held out, for final evaluation

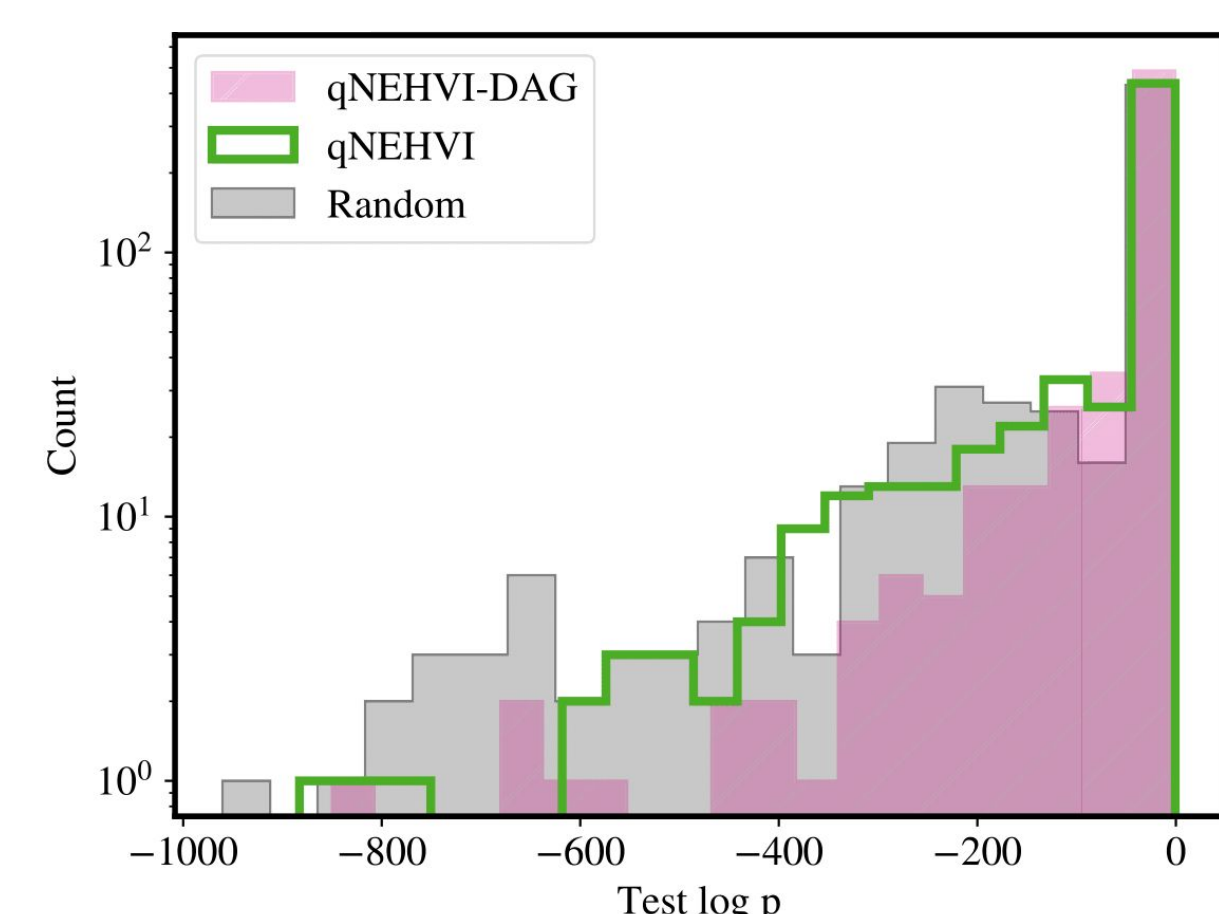


### Joint positives identified over iterations

PropertyDAG-EHVI selection (magenta) identifies significantly more expressing binders relative to standard EHVI (green) and random (gray) selections.

### Log posterior density of joint positives in test set

Surrogate models from PropertyDAG-EHVI (magenta) selection has the most accurate beliefs about the joint positives after the final iteration, relative to standard EHVI (green) and random (gray) selections.



## Summary

- PropertyDAG sits on top of multi-objective BO to make it amenable to a common scenario in drug design, where a hierarchical structure, or partial ordering, exists among the objectives.
- PropertyDAG-BO can identify significantly more designs that are jointly positive (i.e., exceeding a chosen threshold in all properties) than can standard BO.

## References

- [1] Jain et al. (2017). Biophysical properties of the clinical antibody landscape. *PNAS*, 114(5), 944-949
- [2] Raybould et al. (2019). Five computational developability guidelines for therapeutic antibody profiling. *PNAS*, 116(10) 4025-4030

- [3] Emmerich (2005). Single- and multi-objective evolutionary design optimization assisted by Gaussian random field metamodels. *Doctoral dissertation, Dortmund, Univ., Diss., 2005*
- [4] Zitzler et al. 2004. Performance assessment of multiobjective optimizers: An analysis and review. *IEEE Transactions on evolutionary computation*, 7(2), 117-132.

